

**PH4**

Question		Marking details	Marks Available			
1	(a)	Acceleration towards a fixed point [or central / equilibrium](1) and [directly] proportional to the distance from that point (1) Accept $a = -kx$ (1) with $x$ defined	2			
	(b)	Smooth curve drawn which extends at least to $\pm 19.5$ mm [i.e. beyond the extreme points] symmetrically on at least 2 extremes.	1			
	(c)	$\omega = \frac{2\pi}{T} = \frac{2\pi}{0.5} [= 12.57 \text{ rad s}^{-1}]$	1			
	(d)	<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 50%; vertical-align: top;"> <p><b>Either</b></p> <math display="block">v_{\max} = r\omega \text{ [or by impl.] (1)}</math> <math display="block">= 20 \times 10^{-3} \times 12.57</math> <p>[<math>r</math> range 19.5 – 21 mm]</p> <math display="block">= 0.25 \text{ m s}^{-1} \text{ (1)}</math> </td> <td style="width: 5%; border-left: 1px solid black; border-right: 1px solid black;"></td> <td style="width: 45%; vertical-align: top;"> <p><b>Or</b> tangent drawn (1)</p> <math display="block">v_{\max} = \frac{(30 - (-30)) \times 10^{-3}}{0.67 - 0.42}</math> <math display="block">= 0.24 \text{ m s}^{-1} \text{ (1)}</math> </td> </tr> </table>	<p><b>Either</b></p> $v_{\max} = r\omega \text{ [or by impl.] (1)}$ $= 20 \times 10^{-3} \times 12.57$ <p>[<math>r</math> range 19.5 – 21 mm]</p> $= 0.25 \text{ m s}^{-1} \text{ (1)}$		<p><b>Or</b> tangent drawn (1)</p> $v_{\max} = \frac{(30 - (-30)) \times 10^{-3}}{0.67 - 0.42}$ $= 0.24 \text{ m s}^{-1} \text{ (1)}$	2
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(e)	<p>Squaring <math>T = 2\pi\sqrt{\frac{m}{k}}</math> i.e. <math>T^2 = 4\pi^2 \frac{m}{k}</math> or following substitution (1)</p> <p>Substitution (1)</p> <p>Rearranging and answer: <math>k = 6.32 \text{ N m}^{-1}</math></p>	2				
			<b>[8]</b>			

Question		Marking details	Marks Available
2.	(a)	<p>Any 2 × (1) of:</p> <ul style="list-style-type: none"> <li>• forces between molecules negligible [or no forces...] / molecules travel in straight lines between collisions ✓</li> <li>• volume [allow “size”] of molecules negligible / collision time small [cf time between collisions] ✓</li> <li>• molecules behave like perfectly elastically / have elastic collisions ✓</li> <li>• molecules exert forces [or pressure] on walls of container during collisions ✓</li> <li>• gasses consist of a large number of particles / molecules in random motion</li> </ul>	
	(b)	<p>amount of gas, <math>n = \left[ \frac{pV}{RT} = \frac{1.01 \times 10^5 \times (6 \times 5 \times 3)}{8.31 \times 293} \right] = 3730 \text{ mol (1)}</math></p> <p>no. of molecules <math>N = nN_A = 3730 \times 6.02 \times 10^{23} = 2.2 \times 10^{27} \text{ (1)}</math></p>	2
	(c)	$c_{\text{rms}} = \sqrt{\frac{350^2 + 420^2 + 550^2}{3}} \text{ (1) [or by impl.] = } 448 \text{ m s}^{-1} \text{ (1)}$	2
	(d)	<p>Density <math>\rho = (1) \frac{M}{V} = \frac{3733 \times \frac{29}{1000}}{90} [= 1.203 \text{ kg m}^{-3}]</math>.</p> <p>Use of <math>p = \frac{1}{3} \rho \overline{c^2} \text{ (1)}</math>. [<math>c_{\text{rms}} = 502 \text{ m s}^{-1}</math>]. (1)</p> <p>( i.e. use of <math>M/V</math> (1); inserting ~3733 for <math>n</math> (1); relating <math>M</math> to <math>Mr</math> (1); use of <math>p = \frac{1}{3} \rho \overline{c^2}</math> and substitution [or by impl.] (1) )</p>	2
	(e)	<p>(i) Time of travel ~ 0.01 – 0.02 s</p> <p>(ii) No – time estimated is [far] too short (1) e.c.f from (i) Relay is much longer because of collisions between molecules [or equiv. eg takes time to diffuse / mean free path is very short] (1)</p>	1
			2
			<b>[13]</b>

Question		Marking details	Marks Available
3	(a)	$\Delta U =$ increase [accept change / difference] in <u>internal</u> energy [of the gas](1) $Q =$ heat <u>supplied</u> [to] the gas (1) $U =$ work done <u>by</u> the gas (1)	3
	(b)	Readings from graph: $p = 120 \pm 2.5$ kPa; $V = 2.0 \times 10^{-3}$ m (1) $T = \frac{pV}{nR}$ (1) = $\frac{120 \times 10^3 \times 2.0 \times 10^{-3}}{0.1 \times 8.31}$ (1) [= 289 / 290 K]	3
	(c)	Work Done = ‘area’ under graph (1) Any reasonable method used correctly to estimate area, (1) e.g $27 \times 1$ cm squares $\times$ ‘area’ of 1 cm square $\rightarrow$ 169 J <b>or</b> [approximating AB to straight line] area $\sim 1.0 \times \frac{1}{2} \times [120 + 240]$ $\rightarrow 180 \therefore$ a bit less than 180 J $\sim 170$ J.	2
	(d)	(i) $\Delta V = 0$ along AP (1) So $W = p\Delta V = 0$ (1)	2
	(e)	(ii) Work done <b>on</b> gas (1) = $p\Delta V = 240$ J (1)	2
		Temperature at A and B are the same: $U_A = U_B$ so $\Delta U = 0$ , so $Q = W$ [from 1 <sup>st</sup> law] (1) $W$ is different for the two paths so $Q$ is different. (1)	2
			<b>14</b>
4.	(a)	Concentric equipotentials drawn (1) At least 3 outward radial electric field lines drawn symmetrically(1) [No labelling $\rightarrow -1$ ; no arrows on field lines $\rightarrow -1$ ]	2
	(b)	(i) $KE = 8.3 \times 10^{-14}$ J	1
	(ii)	At closest approach, all KE lost [or by impl.] (1) KE lost [or PE gained] = $q\Delta V_E$ (1) $\Delta V = \frac{1}{4\pi\epsilon_0} \frac{Q}{r}$ (1) Subst, manip + ans $\rightarrow r = 1.6 \times 10^{-13}$ m (1) [e.c.f. on KE from (i)]	4
	(iii)	[It retraces its path] with electric PE decreasing (1) and KE increasing (1) or equiv.	2
(iv)	Smooth symmetric curve drawn curving away from nucleus	1	
			<b>10</b>

Question		Marking details	Marks Available
5.	(a)	(i) $\text{N m}^{-2} / \text{Pa}$ [or equiv.] (ii) $\text{Mass} = 1.2 \times 2.0 \times 10^{-4} \times 1.00 \times 10^3$ [= 0.24 kg] (iii) $\text{Change in momentum} = [0 -] 0.24 \times 1.2 \checkmark$ [= -0.29 N s ~ 0.3 N s] (iv) $\text{Force} = \frac{\Delta mv}{t} = \frac{0.3(\text{e.c.f.})}{1} / 0.3 \text{ N}$ [equal and opposite force on wall implied] (1) $\text{Pressure} = \frac{F}{A} = \frac{0.3}{2.0 \times 10^{-4}} = 1500 \text{ Pa}$ [1450 Pa if 0.29 N s used] (1)	1 1 1 2
	(b)	(i) $\lambda = 660 \times 10^{-9} \text{ m}$ [or equiv – unit conversion] (1) $p = \frac{h}{\lambda} = \frac{6.63 \times 10^{-34}}{660 \times 10^{-9}}$ (1) [e.c.f. on unit conv.] = $1.0 \times 10^{-27} \text{ N s}$ (1) (ii) $\text{Photon energy } E = hf = \frac{hc}{\lambda}$ (1) = $3.01 \times 10^{-19} \text{ J}$ [or by impl.] $\text{Number of photons in } 1 \text{ s} = \frac{\text{Power}}{\text{energy of 1 photon}}$ (1) [= $3.32 \times 10^{13}$ ] $\text{Force} = \frac{\Delta p}{t} = 3.32 \times 10^{-12} \text{ N}$ (1) [e.c.f. if only 1 photon used] $\text{Pressure} = 3.3 \times 10^{-6} \text{ Pa}$ (1) [NB $F = \frac{P}{c} \rightarrow$ 1st 3 marks by impl] [If pressure = $1 \times 10^{-21} \text{ Pa}$ given specified “per photon” – or equiv – then 1 mark]	3 4
			<b>[12]</b>

Question		Marking details	Marks Available
6	(a)	$r = 1.0 \times 10^8 \text{ m}$ [unit conversion] (1) $g = \frac{GM_E}{r^2} = \frac{6.67 \times 10^{-11} \times 6.0 \times 10^{24}}{(1.0 \times 10^8)^2}$ (1) [e.c.f. for this mark only] $= 0.04 \text{ N kg}^{-1}$ , Statement “agreement with graph” or equiv (1)	2
	(b)	Moon has a [much] smaller <u>mass</u> than the Earth. [or converse]	1
	(c)	$3.45 [\pm 0.05] \times 10^5 \text{ km}$ (from graph) (1) No resultant gravitational field [or fields of Earth and Moon equal <u>and opposite</u> ] or fields balance at this point. [or equiv](1)	2
	(d)	From M to point of intersection / at start $F_{\text{moon}} > F_{\text{earth}}$ (1) At point of intersection: $F_{\text{moon}} = F_{\text{earth}}$ (1) From point of intersection to earth / at end $F_{\text{earth}} > F_{\text{moon}}$ (1) [- 1 for fields rather than forces; - 1 not using resultant at least once]	3
	(e)	More (1) because gravitational fields of Earth and Moon <u>reinforce</u> [or equiv] and act towards centre of moon <u>opposite to rocket motion</u> . (1) Or [if considering escape from the E/M system] Less because of initial greater PE [less negative] due to Earth’s field.	2
			<b>[11]</b>

Question		Marking details	Marks Available
7.	(a)	$T = 1090 \times 24 \times 60 \times 60 [= 9.42 \times 10^7 \text{ s}]$ [unit conversion] (1) $r_s = \frac{Tv_s}{2\pi}$ (1) or equiv e.g. $v = \frac{d}{t}$ and $d \pi r = 6.82 \times 10^8 \text{ m}$ (1)	3
	(b)	(i) $T = 2\pi \sqrt{\frac{d^3}{G(M_s + M_p)}}$ (equation selection) (1) [or by impl] $(M_s \gg M_p)$ [or by impl] $\rightarrow T = 2\pi \sqrt{\frac{d^3}{GM_s}}$ (1) $d = \sqrt[3]{\frac{T^2 GM_s}{4\pi^2}}$ (rearrangement) (1) [or with numbers] Substitution and convincing calculation(1) [to give = $3.21 \times 10^{11} \text{ m}$ ]	4
		(ii) Use of $M_p = \frac{M_s r_s}{d}$ [in any orientation] or $m_1 r_1 = m_2 r_2$ (1) $= \frac{2.2 \times 10^{30} \times 6.8 \times 10^8}{3.2 \times 10^{11}} = 4.7 \times 10^{27} \text{ kg}$ (1)	2
	(c)	Find $\Delta\lambda$ in star's spectral lines arising from motion of star / Doppler shift (1) Find velocity of star using $\frac{\Delta\lambda}{\lambda} = \frac{v}{c}$	2
			<b>[11]</b>