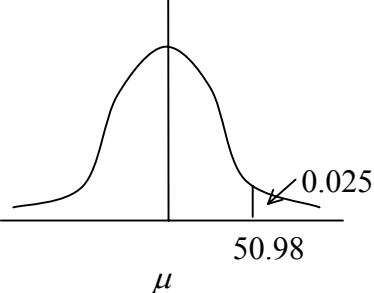
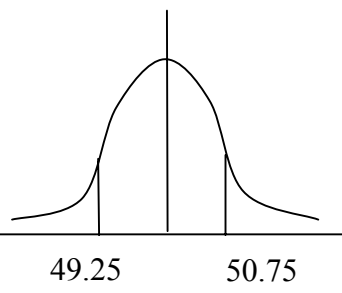
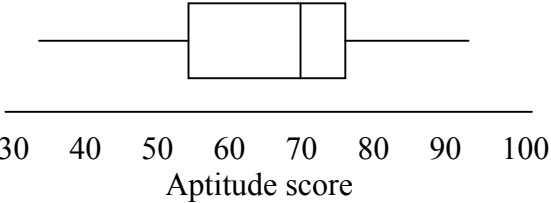


Question Number	Scheme	Marks
<p>1. (a)</p> <p>(b)</p>	<p>Statistical models allow problems to be solved without the need to construct a full-scale physical model, saving time/expense. They allow parameters to be changed and refinements to be made quickly.</p> <p>(i) Normal; (ii) Discrete uniform</p>	<p>B2, 1, 0 (2)</p> <p>B1, B1 (2)</p> <p><b>(4 marks)</b></p>
<p>2. (a)</p> <p>(b)</p>	<p>60A, 40S, 2M</p> $P(\text{all only arts}) = \frac{60}{125} \times \frac{59}{124} \times \frac{58}{123} = \frac{3422}{31775} = 0.10769\dots$ $P(\text{exactly one only science}) = 3 \times \frac{40}{125} \times \frac{85}{124} \times \frac{84}{123}$ $= \frac{2856}{6355} = 0.44940\dots$	<p>B1</p> <p>M1 A1 A1 (4)</p> <p>B1</p> <p>M1 A1 (3)</p> <p><b>(7 marks)</b></p>
<p>3. (a)</p> <p>(b)</p> <p>(c)</p>	$P(A \cap B) = P(A)P(B) = 0.25 \times 0.30 = 0.075$ $P(A \cup B) = P(A) + P(B) - P(A \cap B) = 0.25 + 0.30 - 0.075 = 0.475$ $P(A B') = \frac{P(A \cap B')}{P(B')} = \frac{P(A) - P(A \cap B)}{1 - P(B)}$ $= \frac{0.25 - 0.075}{1 - 0.3}$ $= 0.25$	<p>M1 A1 (2)</p> <p>M1</p> <p>A1 (2)</p> <p>M1</p> <p>M1 A1ft</p> <p>A1 (4)</p> <p><b>(8 marks)</b></p>

Question Number	Scheme	Marks
<p>4. (a)</p>	 <p style="text-align: center;"><math>\mu</math>                      50.98</p> <p style="text-align: center;">0.025</p>  <p style="text-align: center;">49.25                      50.75                      <math>L \sim N(50, 0.5^2)</math></p> <p>(a) <math>P(L &gt; 50.98) = 0.025</math></p> <p><math>P\left(Z &gt; \frac{50.98 - \mu}{0.5}\right) = 0.025</math></p> <p><math>\therefore \frac{50.98 - \mu}{0.5} = 1.96</math></p> <p><math>\therefore \mu = 50</math> (*)</p> <p>(b) <math>P(49.25 &lt; L &lt; 50.75) = P\left(\frac{49.25 - 50}{0.5} &lt; Z &lt; \frac{50.75 - 50}{0.5}\right)</math></p> <p style="padding-left: 100px;"><math>= P(-1.5 &lt; Z &lt; 1.5)</math>                      -1.5 &amp; +1.5</p> <p style="padding-left: 100px;"><math>= 2\Phi(1.5) - 1</math></p> <p style="padding-left: 100px;"><math>= 0.8664</math></p> <p>(c) <math>P(\text{Both}) = (1 - 0.8664)^2</math></p> <p style="padding-left: 40px;"><math>= 0.01784\dots</math></p>	<p>B1</p> <p>M1 A1</p> <p>M1 A1        <b>(5)</b></p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1        <b>(4)</b></p> <p>M1</p> <p>A1        <b>(2)</b></p> <p style="text-align: right;"><b>(11 marks)</b></p>
<p>5. (a)</p>	<p><math>S_{ss} = 108.07875; S_{st} = 129.1675</math></p> <p><math>q = \frac{S_{st}}{S_{ss}} = \frac{129.1675}{108.07875} = 1.1951239\dots</math></p> <p><math>p = \frac{65.0}{8} - (1.951239\dots) \times \frac{48.5}{8} = 0.879561\dots</math></p> <p><math>\therefore t = 0.879561\dots + 1.1951259\dots S</math></p> <p>(b) <math>y - 20 = 0.879561\dots + 1.1951239\dots(x - 6)</math></p> <p style="padding-left: 40px;"><math>\therefore y = 13.709 + 1.195x</math></p> <p>(c) 0.943; the pmcc is an index (no units) and is not affected by linear transformations of either/both variables</p>	<p>B1; B1</p> <p>M1, A1</p> <p>M1, A1</p> <p>A1 ft        <b>(7)</b></p> <p>M1, A1 ft</p> <p>A1        <b>(3)</b></p> <p>B1; B1        <b>(2)</b></p> <p style="text-align: right;"><b>(12 marks)</b></p>

Question Number	Scheme	Marks
<p>6.</p> <p>(a)</p> <p>(b)</p> <p>(c)</p> <p>(d)</p> <p>(e)</p>	$\alpha + \beta = 0.5$ $-2\alpha + 2\beta = -0.2$ $\therefore \alpha = 0.3, \beta = 0.2$ $F(0.8) = 0.6$ $E(X^2) = (4 \times 0.3) + \dots + (4 \times 0.2), = 2.4$ $\therefore \text{Var}(X) = 2.4 - (-0.2)^2, = 2.36$ $E(3X - 2) = 3E(X) - 2, = -2.6$ $\text{Var}(2X + 6) = 4 \text{Var}(X), = 9.44$	<p>B1</p> <p>M1</p> <p>M1 A1; A1 <b>(6)</b></p> <p>B1 ft <b>(1)</b></p> <p>M1, A1</p> <p>M1, A1 <b>(4)</b></p> <p>M1, A1 ft <b>(2)</b></p> <p>M1, A1 ft <b>(2)</b></p> <p><b>(15 marks)</b></p>
<p>7.</p> <p>(a)</p> <p>(b)</p> <p>(c)</p> <p>(d)</p> <p>(e)</p> <p>(f)</p>	<p>Mode = 78</p> <p><math>Q_1 = 56; Q_2 = 70; Q_3 = 78</math></p> <p><math>(Q_3 - Q_1) = 22</math></p> <p><math>Q_1 - 1.0(Q_3 - Q_1) = 34 \Rightarrow 31 \text{ \&amp; } 31 \text{ are outliers}</math></p> <p><math>Q_3 + 1.0(Q_3 - Q_1) = 100 \Rightarrow \text{no outliers}</math></p> <p><i>(accurate sketch on graph paper required)</i></p>  <p>30 40 50 60 70 80 90 100 Aptitude score</p> <p><math>\mu = \frac{3363}{50} = 67.26</math></p> <p><math>\sigma^2 = \frac{238305}{50} - (67.26)^2 = 242.1924</math></p> <p><math>\therefore \sigma = \sqrt{242.1924} = 15.56253\dots</math></p> <p><math>(Q_3 - Q_2) &lt; (Q_2 - Q_1)</math>, i.e. <math>8 &lt; 14 \Rightarrow \text{negative skew}</math></p> <p>Mean &lt; Median &lt; Mode, i.e. <math>67.26 &lt; 70 &lt; 78 \Rightarrow \text{negative skew}</math></p>	<p>B1 <b>(1)</b></p> <p>B1; B1; B1 <b>(3)</b></p> <p>M1 A1</p> <p>A1 <b>(3)</b></p> <p>boxplot M1</p> <p>scales and labels B1</p> <p><math>Q_1, Q_2, Q_3</math> A1</p> <p>31, 32, 34 (39), 92 A1 <b>(4)</b></p> <p>B1</p> <p>M1</p> <p>A1 <b>(3)</b></p> <p>M1, A1</p> <p>M1, A1 <b>(4)</b></p> <p><b>(18 marks)</b></p>